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**B.E / B.Tech ( Full-Time ) DEGREE END SEMESTER EXAMINATIONS, APR / MAY 2014**

**COMMON TO ELECTRONICS AND COMMUNICATION ENGINEERING AND  
BIOMEDICAL ENGINEERING  
III Semester**

**EC 274/ EC 9203 SIGNALS AND SYSTEMS**

(Regulation – 2004/2008)

Time: 3 Hours

Answer ALL Questions

Max. Marks 100

**PART-A (10 x 2 = 20 Marks)**

1. Express discrete time unit step signal in terms of unit impulse signal.
2. Determine the fundamental period for the signal  $x[n]$  given by  $x[n]=e^{j5\pi n}$ .
3. Let  $a_k$  be the Fourier series coefficient of a periodic signal  $x(t)$ . Write the expression for the Fourier series coefficient for the signal  $x(t-t_0)$ .
4. Express the Laplace transform for the signal  $x(t)=e^{-at}u(t)$ .
5. Consider an LTI system with input  $x(t)$  and with response  $y(t)$  defined by the expression  $y(t)=x(t)-x(t-1)$ . Determine the impulse response  $h(t)$  of the LTI system.
6. State Sampling theorem.
7. Consider an LTI system defined by the transfer function  $H(s)=\frac{1}{s^2+3s+2}$  ;  
Determine the poles and zeros.
8. Express the z-transform for the signal  $y[n]=\delta[n]-\delta[n-1]$ .
9. Consider the impulse response of an LTI system as  $h[n]=\delta[n]-\delta[n-1]$ . Determine the response  $y[n]$  if the input  $x[n]$  to the LTI system is  $u[n]$ .
10. Consider the LTI system described by the transfer function  $H(z)=\frac{z^3+1}{z^2+z+1}$ . State whether the system is causal or not with justification.

**PART-B (5 x 16 = 80 Marks)**

11. i. Consider a system whose input  $x(t)$  and output  $y(t)$  are related by the following expression.  $y(t)=x(t-1)-x(2-t)$ . Determine whether the system satisfies the following properties with justification  
(a) Memoryless  
(b) Time invariant  
(c) Linear  
(d) Causal. (8)
- ii. Consider the signal  $x(t)=e^{-2t}u(t)$ .  
(a) Plot the signal  $x(t)$  and  $x(-t)$   
(b) Determine  $P_\infty$  and  $E_\infty$  (8)

12. a. i. Calculate the Fourier series coefficient for the continuous time periodic signal  $x(t) = \begin{cases} 1, & 0 < t < 1 \\ -1 & 1 < t < 4 \end{cases}$ , with fundamental frequency  $\omega = \pi/2$ . (8)

ii. Determine the Laplace transform for the signal  $x(t) = 2e^{-2t}u(t) - 4e^{-t}u(-t)$  and plot the region of convergence. (8)

(OR)

12. b. i. Consider a rectangular pulse signal  $x(t) = \begin{cases} 1, & |t| < T_1 \\ 0, & |t| > T_1 \end{cases}$ . Determine its Fourier transform and plot its spectrum. (8)

ii. Compute the Fourier transform for the signal  $x(t) = e^{-a|t|}u(t)$  with  $a > 0$ . Plot its spectrum. (8)

13 a. i. Let  $x(t) = u(t-2) - u(t-4)$  and  $h(t) = e^{-4t}u(t)$ . Compute the convolution of  $x(t)$  and  $h(t)$ . (8)

ii. Consider an LTI system with system function  $H(s) = \frac{s-1}{(s+1)(s-4)}$ , determine the impulse response  $h(t)$ , if the system is causal. (8)

(OR)

13. b. i. Consider an LTI system with input  $x(t) = e^{-2t}u(t)$  and output  $y(t) = [e^{-t} - e^{-4t}]u(t)$ . Determine the transfer function  $H(s)$ . Using  $H(s)$ , state whether the system is causal and/or stable with justification. (8)

ii. Let  $x(t) = e^{-2t}u(t)$  and  $h(t) = u(t)$ . Compute the convolution of  $x(t)$  and  $h(t)$ . (8)

14 a. i. Compute the Fourier transform for the signal  $x[n] = u[n-2] - u[n-6]$  (8)

ii. Consider the signal  $x[n] = \begin{cases} \left(\frac{1}{3}\right)^n \cos\left(\frac{\pi}{4}n\right), & n \leq 0 \\ 0, & n > 0 \end{cases}$ , evaluate the z-transform and plot the region of convergence. (8)

(OR)

14 b. i. Compute the Fourier transform for the signal  $x[n] = \begin{cases} n, & -3 \leq n \leq 3 \\ 0, & \text{otherwise} \end{cases}$  (8)

ii. Consider the signal  $x[n] = \left(\frac{1}{5}\right)^n u[n-3]$ , evaluate the z-transform and plot the region of convergence. (8)

15 a. i. Compute the convolution of  $x[n]$  and  $h[n]$  where  $x[n]$  and  $h[n]$  are defined by

$$\begin{aligned} x[n] &= \begin{cases} 1, & 3 \leq n \leq 8 \\ 0, & \text{otherwise} \end{cases} \\ h[n] &= \begin{cases} 1, & 4 \leq n \leq 15 \\ 0, & \text{otherwise} \end{cases} \end{aligned} \quad (12)$$

ii. Consider the difference equation  $y[n] - 1/4y[n-1]=x[n]$  relating the input  $x[n]$  and output  $y[n]$  of a causal LTI system. Determine the transfer function  $H(z)$  of the system. (4)

(OR)

15 b. Consider a causal LTI system described by the transfer function

$$H(z) = \frac{\left(1 + \frac{1}{4}z^{-1}\right)\left(1 - 2z^{-1}\right)}{\left(1 - \frac{1}{4}z^{-1}\right)\left(1 + \frac{1}{2}z^{-1}\right)},$$

i. Mark the poles and zeros in the  $z$ -plane and show the region of convergence and determine the impulse response  $h[n]$ . (8)

ii. Represent the block diagram for  $H(z)$  using direct form II realization. (8)