

16/05/19

[F.T]

B. E. DEGREE EXAMINATION, April/May 2019.

College of Engineering, Anna University

Subject: EE8402 DIGITAL SIGNAL PROCESSING

Branch: Electrical and Electronics Engineering; Regulation 2012

Time: Three hours

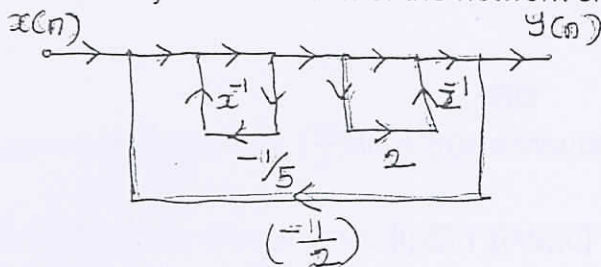
Answer ALL questions

Max.Marks : 100

PART - A

(10x2 = 20)

- Determine whether  $y(n) = 2x(n)+3$  is casual and linear.
- Find the impulse response of the system described by the difference equation.  
 $y(n) = x(n)+2x(n-1)+x(n-2)$
- Sketch the unit sample response of a linear shift invariant system with  $h(n) = a^n u(n)$  with  $|a| < 1$ .
- Find the Z transform of  $x(n) = u(n)$
- Find the discrete fourier series representation for the sequence  $x(n) = \sum_{k=-\infty}^{\infty} x(n - 10k)$  where  $x(n) = 1 \quad 0 \leq n < 5$   
 $0 \quad \text{else}$
- Find  $x(n) = x_1(n) * x_2(n)$  where  $x_1(n) = x_2(n) = 1 \quad 0 \leq n \leq n - 1$   
 $0 \quad \text{else}$
- The system function of an FIR filter is  $H(Z) = (1+0.2Z^{-1}+0.8Z^{-2})$ . Find a linear phase system that has a frequency response with the same magnitude as that of  $H(Z)$ .
- Find the system function of the network shown in fig.



- An analog butterworth filter is described by the transfer function  $H(s) = \frac{1}{1+(\frac{s}{\omega_c})^2}$ . Find the transfer function of the digital Butterworth filter with  $\omega_c = 0.25\pi$  rad. (use impulse invariant technique).
- Determine the order of the low-pass butterworth filter that has a 3.dB cut off frequency of 1kHz and an attenuation of 40dB at 2kHz.

PART – B

(5x16 = 80)

11. a) (i) Test the stability of the first order IIR filter governed by the equation  
 $y(n) = x(n) + b y(n-1)$ ,  $|b| < 1$  (10)
- (ii) Determine the unit step response of the I order difference equation.  
 $y(n) + a y(n-1) = x(n)$   $|a| < 1$  (6)

- 12.(a) (i) Determine the Z-transform of
- 1)  $\sin(\omega_0 n)$  (5)
  - 2)  $n u(n)$  (5)
- (ii) Using residue method, find the inverse Z-transform of  
 $X(z) = \frac{1}{(z-0.25)(z-0.5)}$  ROC :  $|z| > 0.5$  (6)

OR

12(b) A causal system is represented by the following difference equation

$$Y(n) + \frac{1}{4} y(n-1) = x(n) + \frac{1}{2} x(n-1)$$

- Find (i) System transfer function  $H(z)$  (3)
- (ii) Plot the poles and zeros (3)
- (iii) Unit sample response (5)
- (iii) Frequency response of the system (5)



13 (a) Using DFT and IDFT compute the circular periodic convolution of the two sequences.

$$x_1(n) = \{1, 1, 2, 2\}$$

$$x_2(n) = \{1, 2, 3, 4\}$$

OR

- 13(b) (i) Find the 4 point DFT of the sequence  $x(n) = \sin\left(\frac{n\pi}{4}\right)$  and sketch the magnitude and phase spectrum. (8)
- (ii) Determine the IDFT of  $X(k) = \{3, (2+j), 1, (2-j)\}$  using 4 point decimation in time FFT technique. (8)
- 14.a) Using Decimation in frequency FFT algorithm compute DFT for  $x(n) = \{1, 0, 0, 0, 0, 0, 0, 0\}$

OR

14 b) Consider the causal linear shift invariant filter with system function.

$$H(z) = \frac{1+0.875z^{-1}}{(1+0.2z^{-1}+0.9z^{-2})(1-0.7z^{-1})}$$

Draw a signal flow graph for this system using

- |                   |     |     |
|-------------------|-----|-----|
| 1. Direct form I  | (3) | (3) |
| 2. Direct form II | (3) | (3) |
| 3. Cascade form   | (4) | (5) |
| 4. Parallel form. | (4) | (5) |

15.a) Using frequency sampling technique design a linear phase low pass filter with the following specifications  $\omega_c = \pi/4$  rad/sec. and  $N=15$  and plot the magnitude response.

OR

15b) Design a digital FIR high pass filter with the following frequency response.

$$H(e^{j\omega}) = 1 \text{ for } \pi/4 \leq \omega \leq \pi$$

$= 0$  for  $|\omega| \leq \pi/4$  of length  $N=11$  using Hanning window. Give the filter transfer function.

